Experimental Search for Spin-Dependent (and Independent) Forces in the Sub-mm range

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Parameterization and Existing Limits

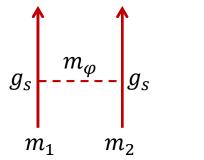
Experimental Approach

Projected Sensitivity

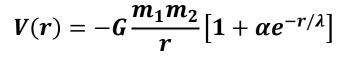
Recent Data and Current Sensitivity (spin-independent)

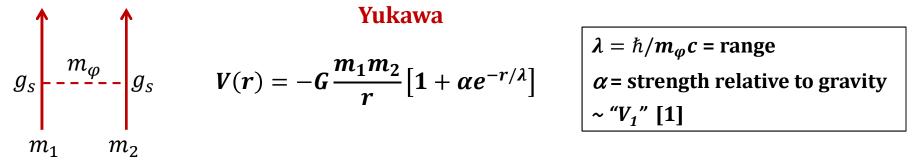
Spin-Polarized Test Mass R&D

Parameterization



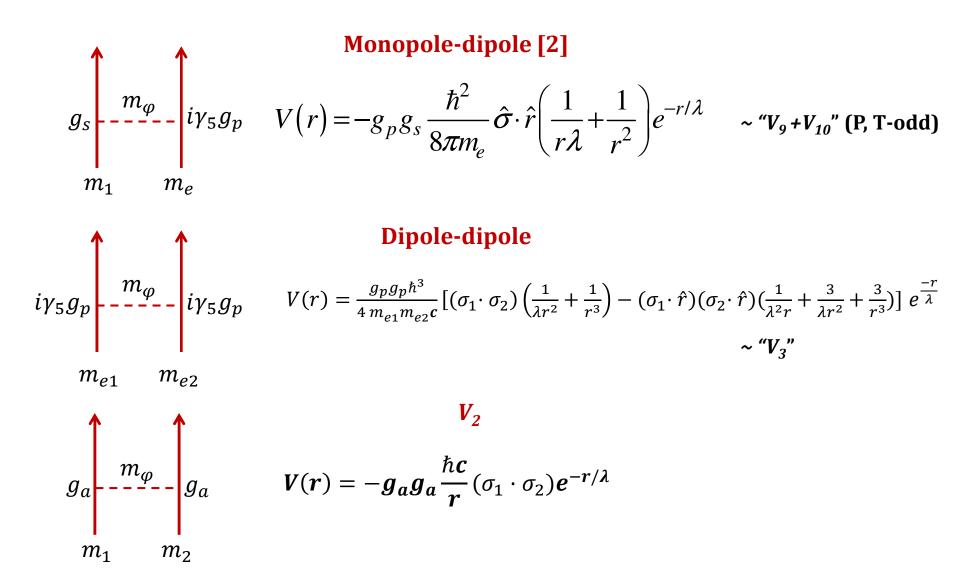






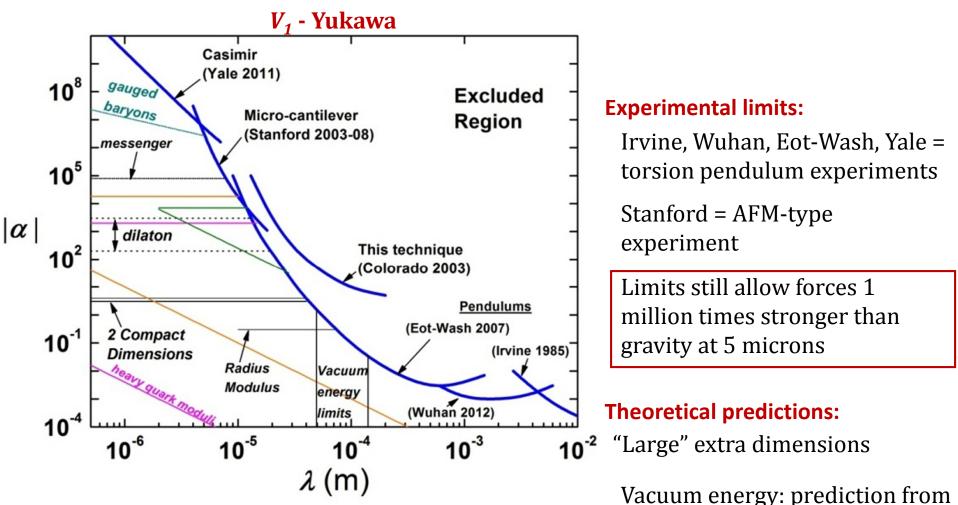
[1] B. Dobrescu and I. Mocioiu, J. High Energy Phys. 0611, 005 (2006)

Spin-Dependent Interactions



[1] B. Dobrescu and I. Mocioiu, J. High Energy Phys. 0611, 005 (2006)[2] J. E. Moody and F. Wilczek, Phys. Rev. D 30, 130 (1984)

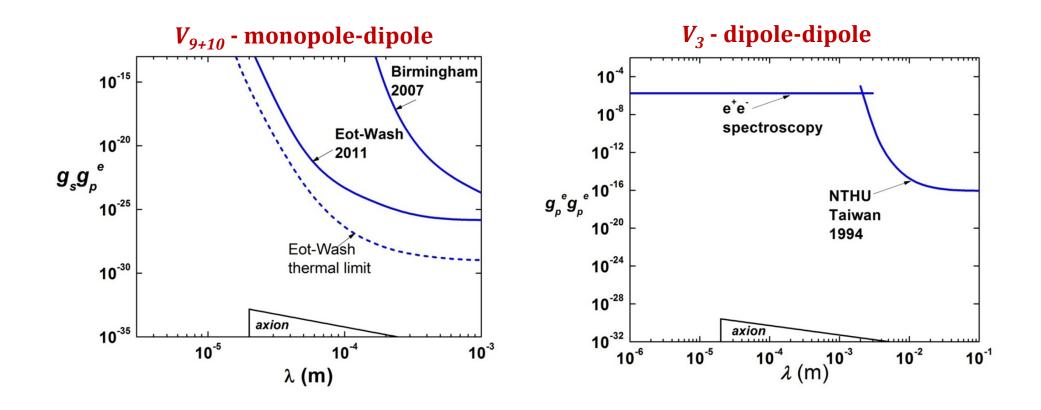
Direct Experimental Limits and Predictions



Irvine: J. Hoskins et al., PRD 32 (1985) 3084 Wuhan: S-Q. Yang et al., PRL 108 (2012) 081101 Eot-Wash: D. Kapner et al., PRL 98 (2007) 021101 Stanford: A. Geraci et al., PRD 78 022002 (2008) Yale: A. Sushkov et al., PRL 107 (2011) 171101 [APS: H12 – 1] Vacuum energy: prediction from new field which also keeps cosmological constant small

Moduli, dilatons: new particles motivated by string models

Direct Experimental Limits and Predictions



Eot-Wash: S. Hoedl et al., PRL 106 (2011) 041801 NTHU: W-T. Ni et al., Physica B 194 (1994) 153 e⁺e⁻: A. Mills, PRA 27 (1983) 262; M. Ritter et al., PRA 30 (1984) 1331

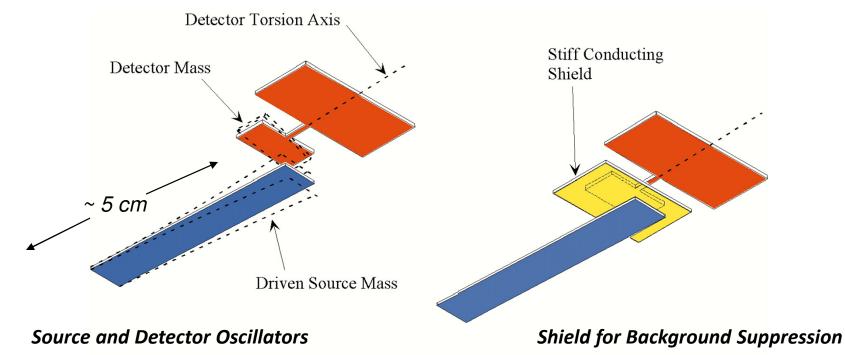
Experimental Approach

Planar Geometry - null for 1/r²

Resonant detector with source mass driven on resonance

1 kHz operational frequency - simple, stiff vibration isolation

Double-rectangular torsional detector: high Q, low thermal noise



Stiff conducting shield for background suppression

Central Apparatus

Vibration isolation stacks: Brass disks connected by fine wires; soft springs which attenuate at $\sim 10^{10}$ at 1 kHz (reason for using 1 kHz)

Readout: capacitive transducer and lock-in amplifier

Vacuum system: 10⁻⁷ torr

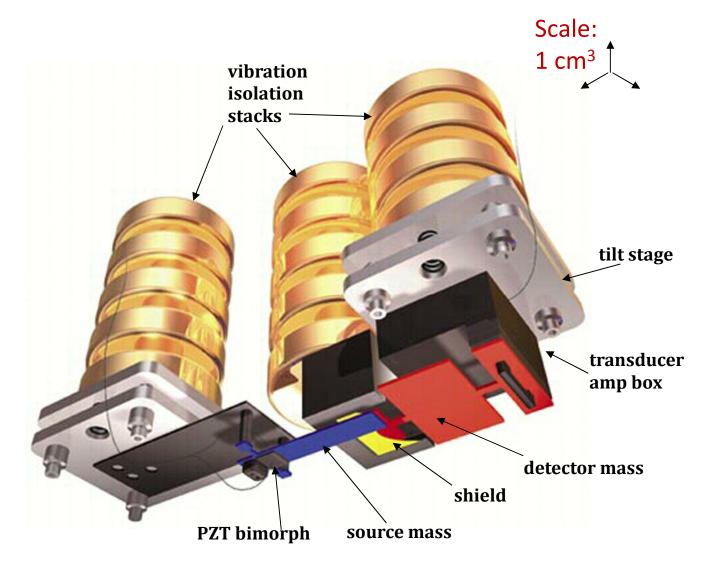
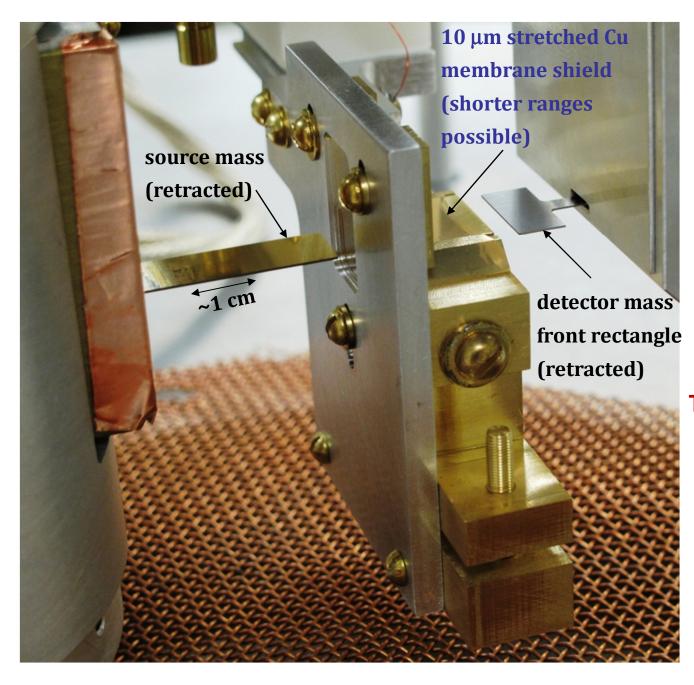


Figure: Bryan Christie (www.bryanchristie.com) for Scientific American (August 2000)

Interaction Region



Thinner shield

 $60\,\mu m$ thick sapphire plate replaced by $10\,\mu m$ stretched copper membrane

Compliance ~5x better than needed to suppress estimated electrostatic force

Minimum gap reduced from 105 μ m (2003) to 40 μ m.

Sensitivity: increase Q and statistics, decrease T

• Yukawa signal: Force on detector due to Yukawa interaction with source

 $F_{Y}(t) \approx 2\pi\alpha G\rho_{s}\rho_{d}A_{d}\lambda^{2} \exp(-d(t)/\lambda)[1-\exp(-t_{s}/\lambda)][1-\exp(-t_{d}/\lambda)]$ ~ 3 x 10⁻¹⁵ N (for $\alpha = 1, \rho = 20$ g/cc, $\lambda = 50$ µm)

- Spin-dependent: Integrate V₂, V₃, monopole-dipole numerically with:
 - $\sim cm^2 \, x \, 100 \, \mu m$ spin-polarized samples on test masses
 - $n_s = 10^{21}/\text{cc} (10\% \text{ of world record } [1])$
- Thermal Noise

$$F_{T} = \sqrt{\frac{4\kappa TD}{\tau}} \qquad D = \frac{\omega m}{Q}$$

~ 3 x 10⁻¹⁵ N rms (300 K, Q = 5 x10⁴, 1 day average)
~ 7 x 10⁻¹⁷ N rms (4 K, Q = 5 x10⁵, 1 day average)

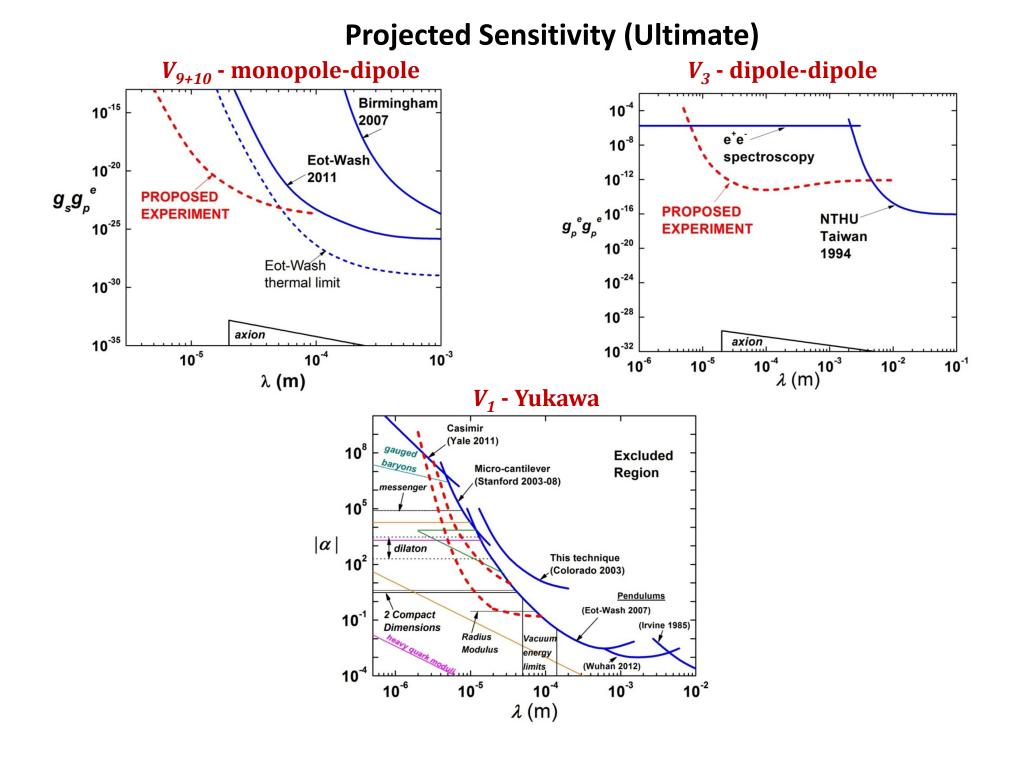
AITTO

• Setting SNR = 1 yields

$$lpha \sim rac{1}{
ho^2} \sqrt{rac{kTm\omega}{Q au}} \qquad gg \sim rac{1}{n^2} \sqrt{rac{kTm\omega}{Q au}}$$

[1] W-T. Ni et al., Physica B 194 (1994) 153

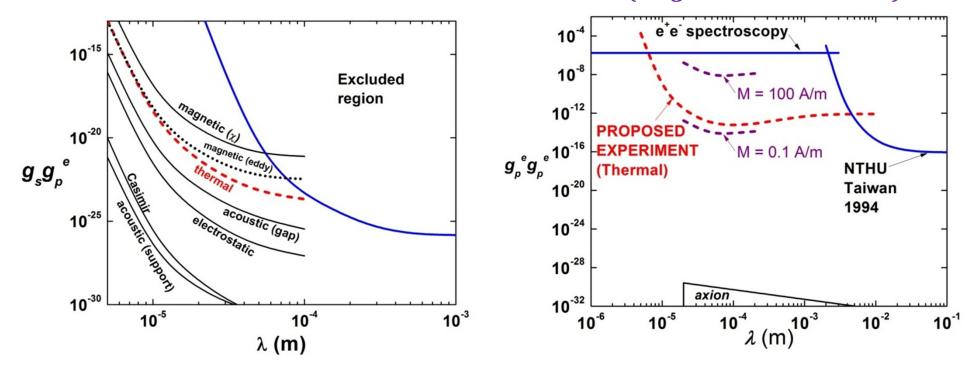
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Other Backgrounds

 V_{9+10} - monopole-dipole

*V*₃ - dipole-dipole (magnetic contaminants)

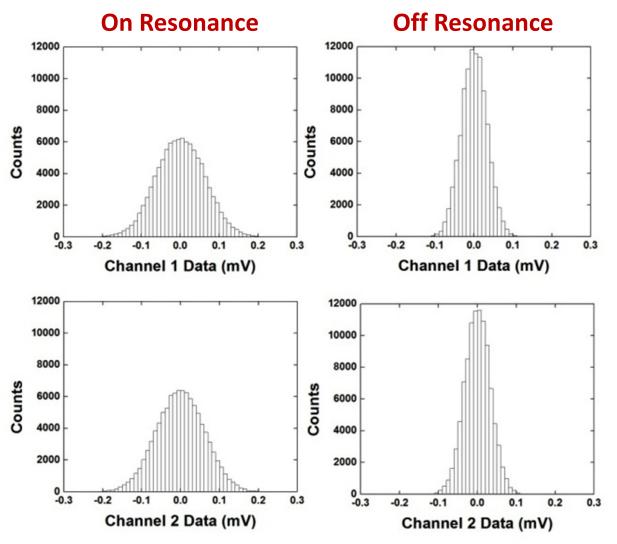


Spin-Independent Force Measurement Data – March 2012

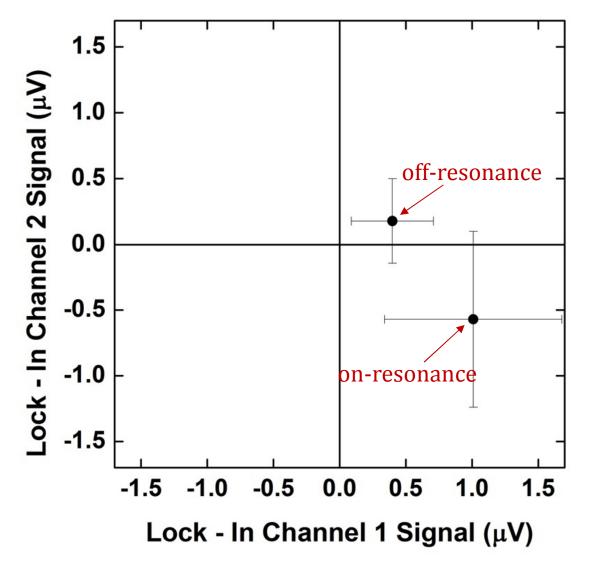
19 hours on-resonance data collected over 3 days with interleaved diagnostic data

On-resonance: Detector thermal motion and amplifier noise

Off-resonance: amplifier noise



Force Measurement Data - Detail



Net Signal:

$$V_{on} - V_{off} = 0.93 \pm 0.74 \,\mu V \,(1\sigma)$$

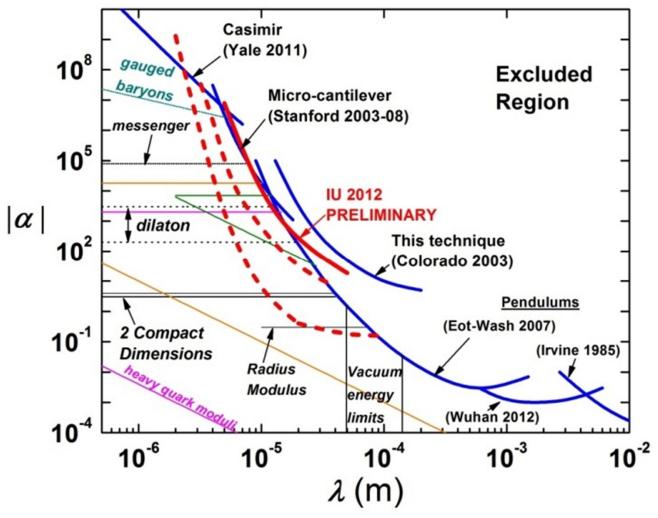
Force:

 $F = 4.0 \pm 3.2 \text{ fN}$

Possible Source:

Detector – *probe* force from ~ nV scale "ground" fluctuations on detector mass

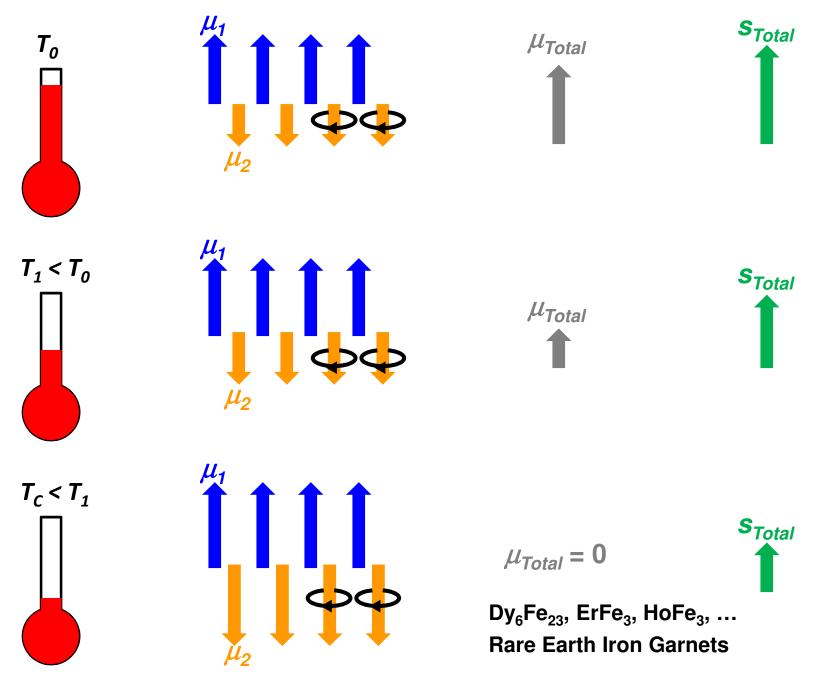
Current Limits (2σ)



Minimum gap: 55 ± 6 μm assumes 10 μm shield flat (optimistic)

Assumes phase of Yukawa force in direction of maximum signal (pessimistic; not yet measured)

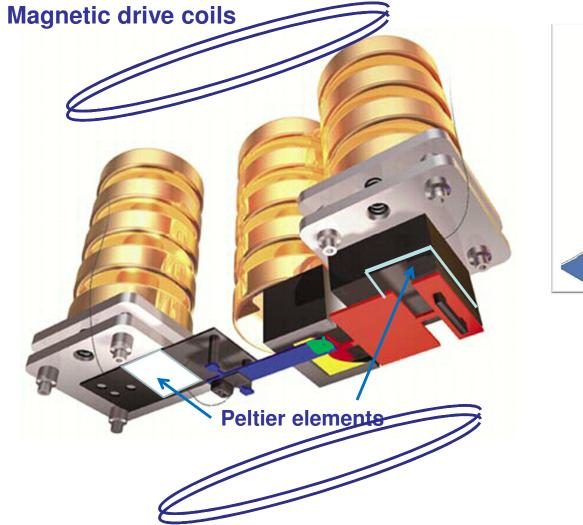
Compensated Ferrimagnet

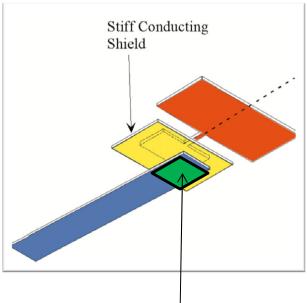


Spin-Dependent Apparatus

Adapt current apparatus

- Cool to *T*_{comp} with thermoelectric elements
- Drive test masses with AC magnetic field until *T*_{comp} (no magnetization)

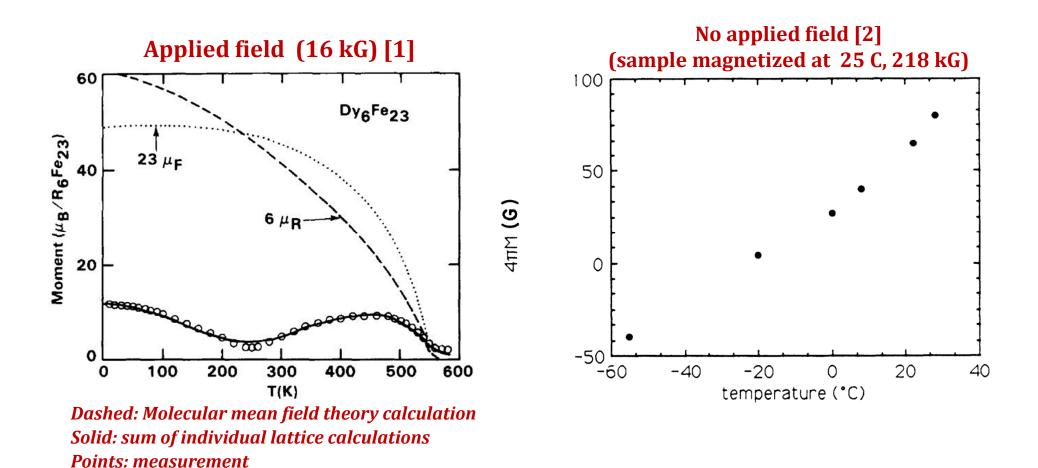




- Dy₆Fe₂₃ test mass 100 μm thick
- Magnetic shield 100μm, μ-metal?

Dy_6Fe_{23} – Magnetization vs T

• $T_c \approx 250$ K (Cool with shield, chiller, thermoelectric elements)

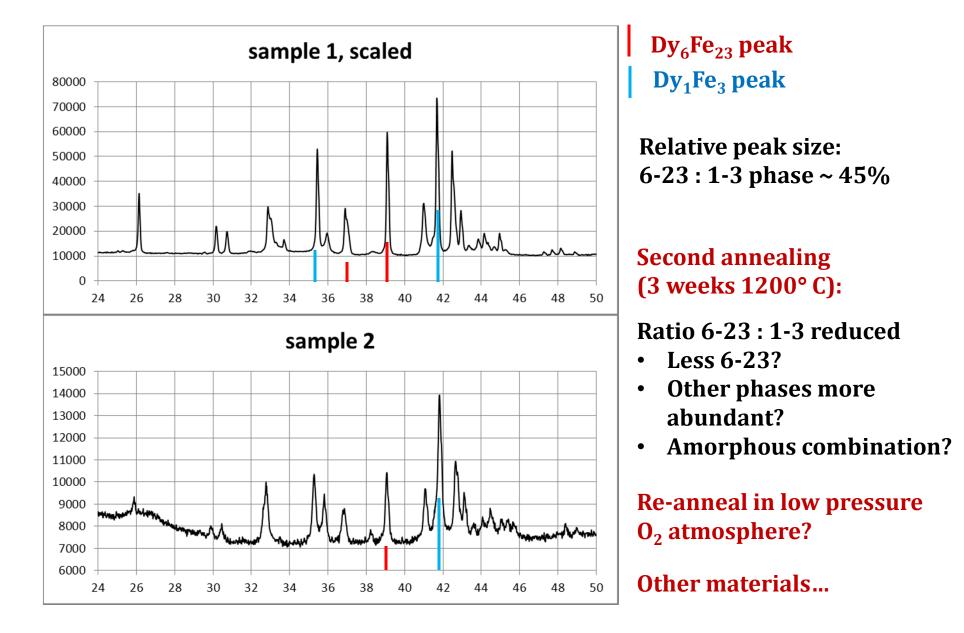


[1] J. Herbst, J. Croat, J. Appl. Phys. 55 (1984) 3023.

[2] R. Ritter, C. Goldblum, W.-T. Ni, G. Gillies, C. Speake, PRD 42 (1990) 977.

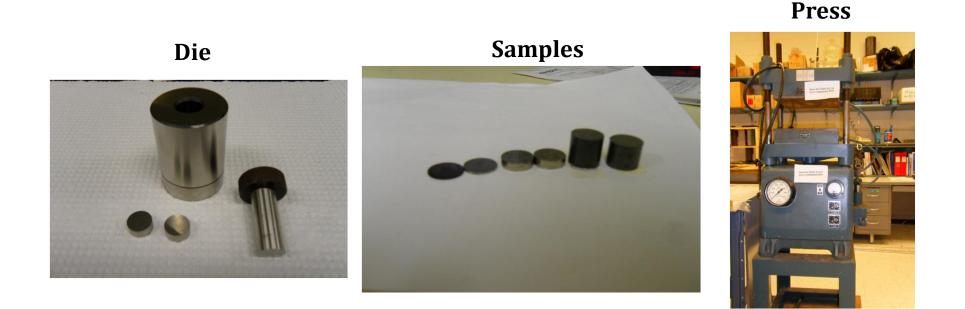
Dy₆Fe₂₃ Production (Ames National Lab)

- Melt 20.7 / 79.3 wt.% Dy/Fe in furnace
- Anneal several days at 1200°C
- X-Ray diffraction analysis:



Dy_6Fe_{23} sample fabrication - Pressing test samples

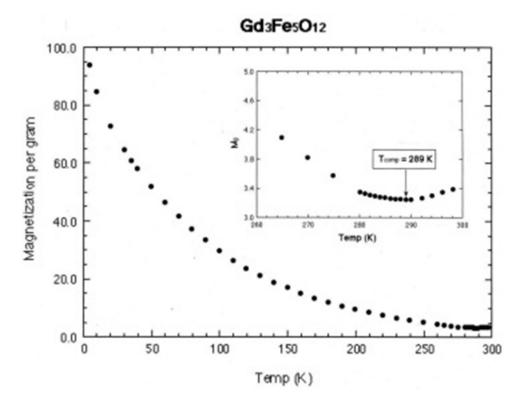
- 1. Metallic powder + binder (2g paraffin in heptane, or 10% Cereox powder)
- 2. Pour mixture into die, press hydraulically at 3000 psi
 - Robust sub-millimeter samples (Fe) routinely attainable
 - Goal: Repeat procedure with ferrimagnet



Next step: Magnetize in strong field, measure magnetization versus temperature

Rare-Earth Iron Garnets

Geselbracht, et al., J. Chem. Edu. 71 (1994) 696



Combine 1 M Dy(NO₃)₃·6H₂O with 1 M FeCl₃·6H₂O Add NaOH dropwise to precipitate solid Decant solution, wash & dry solid Press into pellet Bake at 900 C in air 18-24 h

Summary and Outlook

High-frequency experiment currently excludes spin-independent forces > 10⁵ times gravitational strength above 10 microns

Sensitive to forces 1000 times gravitational strength at 10 microns

Reduce metrology uncertainties

Understand, reduce "probe-force" background

Chameleon Analysis (2003 data)

Cryogenic experiment with gravitational sensitivity at 20 microns proposed

Demonstrate cryogenic transducer and thermal noise below 10 K

Spin-dependent experiments with same technique potentially ~ 8 orders of magnitude more sensitivity than current experiments (thermal noise limit); 3-5 orders more sensitive with reasonable magnetic backgrounds

Find a pure ferrimagnet and demonstrate 200 < Tc < 300 (candidates exist)

Fabricate flat samples, attach to test masses

Assemble cooling system

Demonstrate stimulated magnetic forces at T > Tc

Collect data at Tc

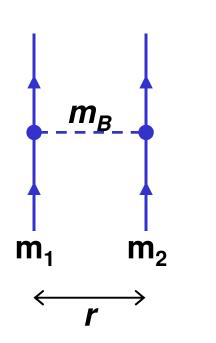
Restore thicker shield (if needed), investigate high permeability layers

(Supplemental Slides)

Parameterization

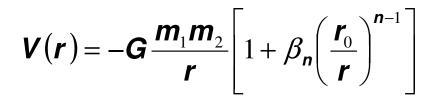
Yukawa Interaction

Power Law

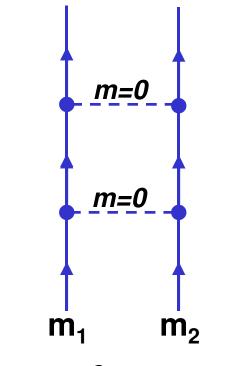


$$\boldsymbol{V}(\boldsymbol{r}) = -\boldsymbol{G} \frac{\boldsymbol{m}_1 \boldsymbol{m}_2}{\boldsymbol{r}} \left[1 + \alpha \boldsymbol{e}^{-\boldsymbol{r}/\lambda} \right]$$

 $\lambda = \hbar / m_B c = range$ $\alpha = strength relative$ to gravity



 r_0 = experimental scale



set limits on β_n for n = 2 - 5

Signals in Recent Data

Pre-2010: ~10 x thermal noise (10³ s), non-resonant

• electronic pick-up, switched to differential amplifier

Spring 2010: ~ 5x thermal noise (10³ s), resonant, position independent

• Vibration, replaced stacks

Summer/fall 2010: ~ 2-5 x thermal noise, resonant, weak gap dependence

• "long-range" capacitive coupling, re-designed shield

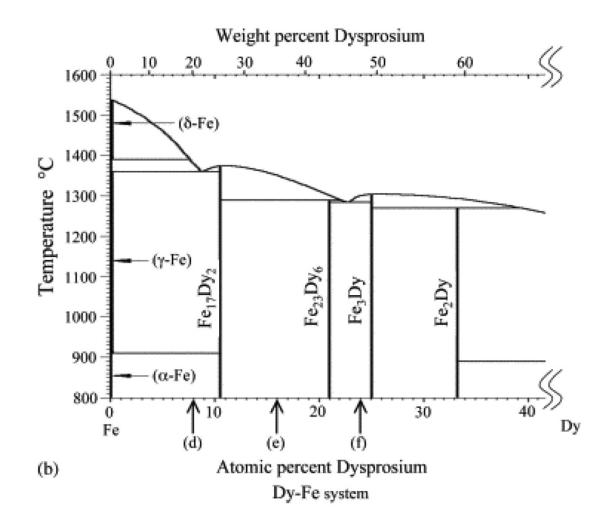
Spring/summer 2011: ~ 2-5 x thermal noise, resonant, smallest gaps

• Poorly-grounded shield or the problem below (?)

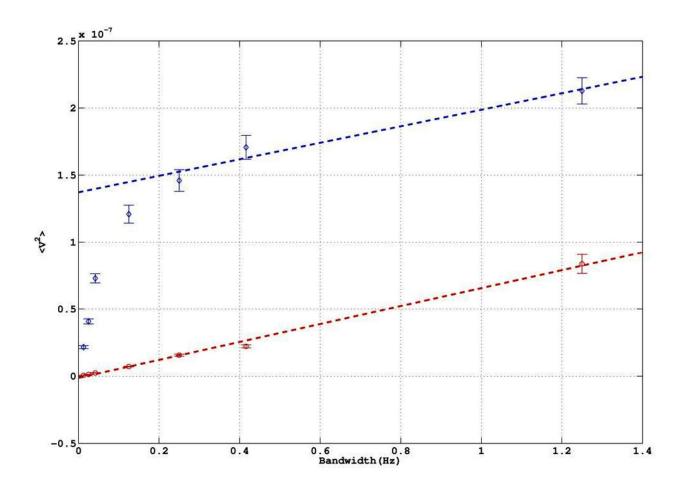
Fall 2011: fluctuating resonant signals and noise

• Faulty (?) differential input on lock-in

Dy-Fe Phase Diagram



Thermal and Amplifier Noise



 $G = 20k \rightarrow amp \sim 10 nV/\sqrt{Hz}$

Calibration with Thermal Noise

Free thermal oscillations:

$$\frac{1}{2}k_BT = \frac{1}{2}m\omega^2 z_{T(rms)}^2$$

Damped, driven oscillations on resonance:

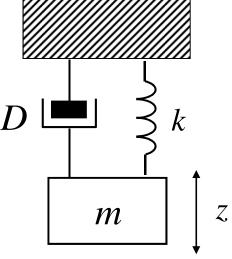


$$\Rightarrow \text{Measured force: } F_D = -\frac{\overline{z_D}}{z_{T(rms)}} \frac{\omega \sqrt{mk_B T}}{Q}$$

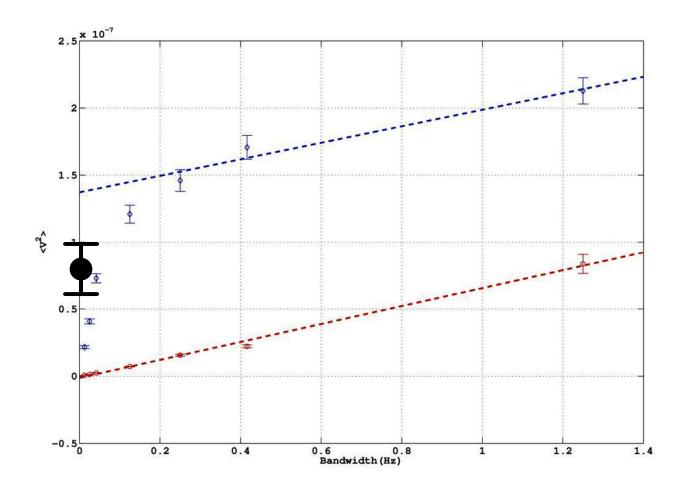
$$z_T, z_D, \omega, T, Q$$
 from data, $\frac{\overline{z_D}}{z_{T(rms)}} = \frac{\overline{V_D}}{V_{T(rms)}}$

For distributed oscillator sampled at $r, m \rightarrow \frac{\rho \int |z|^2 dV}{|z(r)|^2}$ mode shape from computer model

Detector Model:

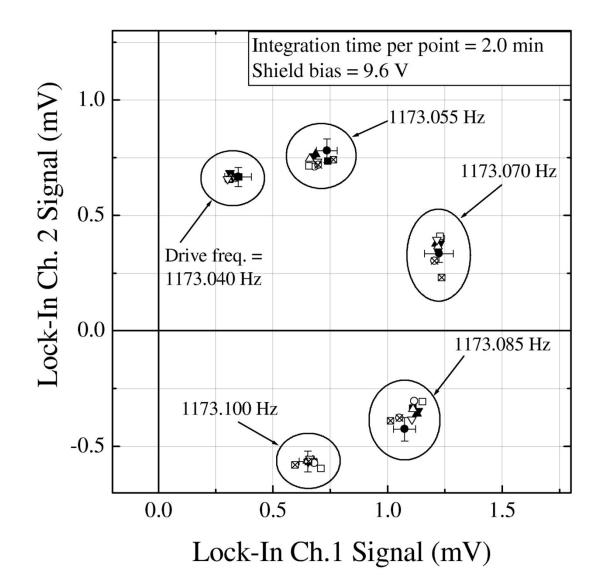


Thermal and Amplifier Noise



 $G = 20k \rightarrow amp \sim 10 nV/\sqrt{Hz}$

Diagnostic Data – Shield Biased



Analysis steps

Likelihood function:

$$L(x \mid \alpha, \nu) = \left(\frac{1}{\sigma\sqrt{2\pi e}}\right)^{N} \exp\left[\frac{-(\overline{x} - \mu(\alpha, \nu))^{2}}{2(\sigma/\sqrt{N})^{2}}\right]$$

 \bar{x} = average voltage measured, σ = standard deviation, N = number of samples $\mu(\alpha, v)$ = predicted voltage for given α and set of systematics v

General expression for predicted average voltage:

$$\mu(\alpha, \nu) = \sqrt{|V^{T}|^{2}} \frac{Q}{\omega_{0}\sqrt{k_{B}T\rho_{d}}} \frac{\int d^{3}\vec{r}'\vec{z}^{F}(\vec{r}') \bullet \vec{f}(\vec{r}')}{\sqrt{\int d^{3}\vec{r}' |\vec{z}^{F}(\vec{r}')|^{2}}}$$

 V^{T} = thermal noise voltage fluctuations

Q = detector mechanical quality factor

 ω_0 = detector resonant frequency

 ρ_d = detector mass density

 $z^{F}(r')$ = displacement of detector at arbitrary point in detector r'

f(r') = force/unit volume on detector at arbitrary point in detector r'

Analysis steps

Interval [α_{lo} , α_{up}] that contains true α with probability CL:

$$CL = \int_{\alpha_{lo}}^{\alpha_{up}} p(\alpha \mid x) d\alpha$$

 $p(\alpha|x)$ = probability density function for α given DATA x

(For any λ , find [α_{lo} , α_{up}] so that CL = 0.95)

e.g., for
$$\lambda$$
 = 20 µm, -6 x 10³ < α < 4 x 10³

Bayes' Theorem:

$$p(\alpha \mid x) = \frac{L(x \mid \alpha)\pi(\alpha)}{\int_{-\infty}^{\infty} L(x \mid \alpha')\pi(\alpha')d\alpha'}$$

 $L(\alpha|x)$ = likelihood function INTEGRATED OVER SYSTEMATICS v $\pi(\alpha)$ = prior pdf for α (assumed uniform between old limits on α)

Analysis steps

Monte Carlo program calculates:

$$\int d^{3}\vec{r}'\vec{z}^{F}(\vec{r}')\bullet\vec{f}(\vec{r}')$$

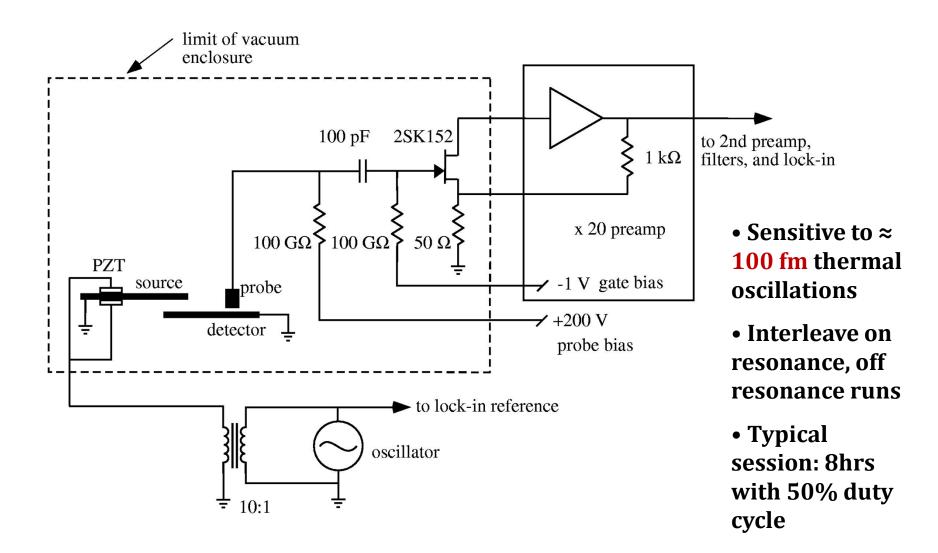
 $z^{F}(r')$ = displacement of detector at arbitrary point r' in detector

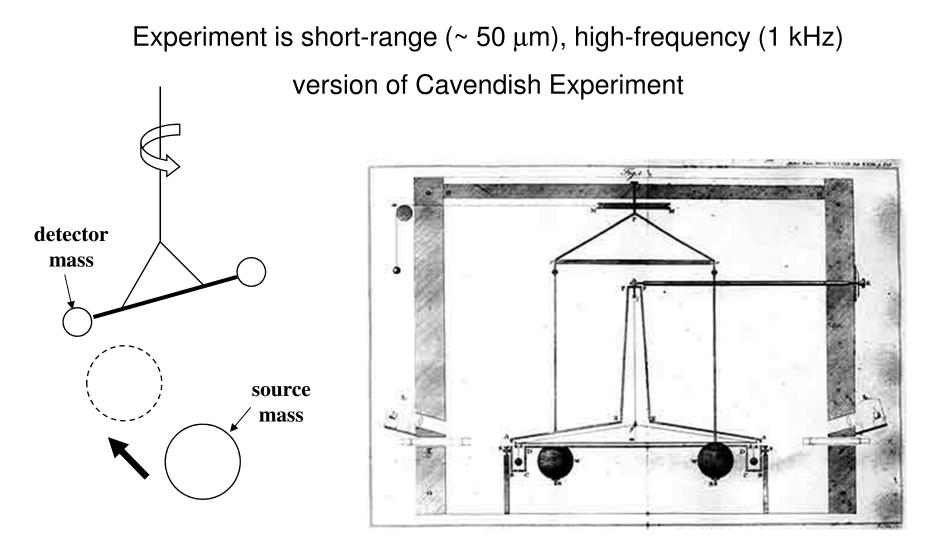
(given by 2nd order polynomial fit to geometry survey data)

f(r') = force/unit volume on detector at arbitrary point r' in detector

What is f(r') due to interaction with source mass for case of LLV force?

Readout



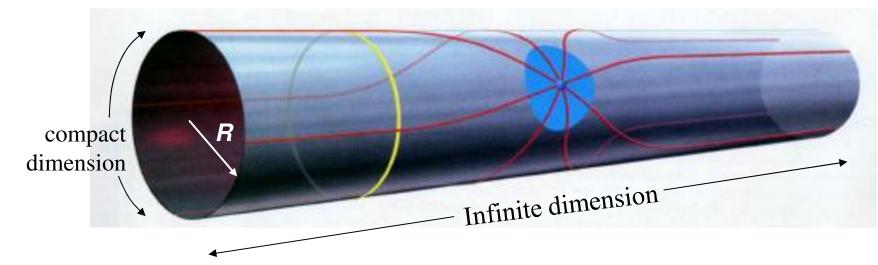


Pb test masses ($\rho = 11000 \text{ kg/m}^3$): large = 20 cm diam., small = 5 cm diam

$$G = 6.76 \text{ x } 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$$

2006 CODATA: G = 6.67428(67) x 10^{-11} m³ kg⁻¹ s⁻²

"Large" Extra Dimensions



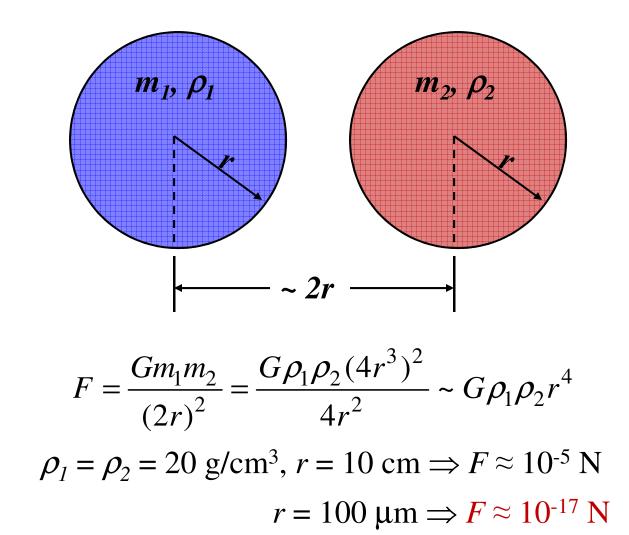
Strong, Weak, EM force confined to 3 dimensions

• Gravity spreads out into *n* extra dimensions of size *R*, appears diluted

$$\boldsymbol{R} = \left[\frac{\boldsymbol{M}_{\boldsymbol{P}}}{\boldsymbol{M}^{\star}}\right]^{2/n} \left[\frac{\hbar}{2\pi \boldsymbol{M}^{\star}}\right]$$

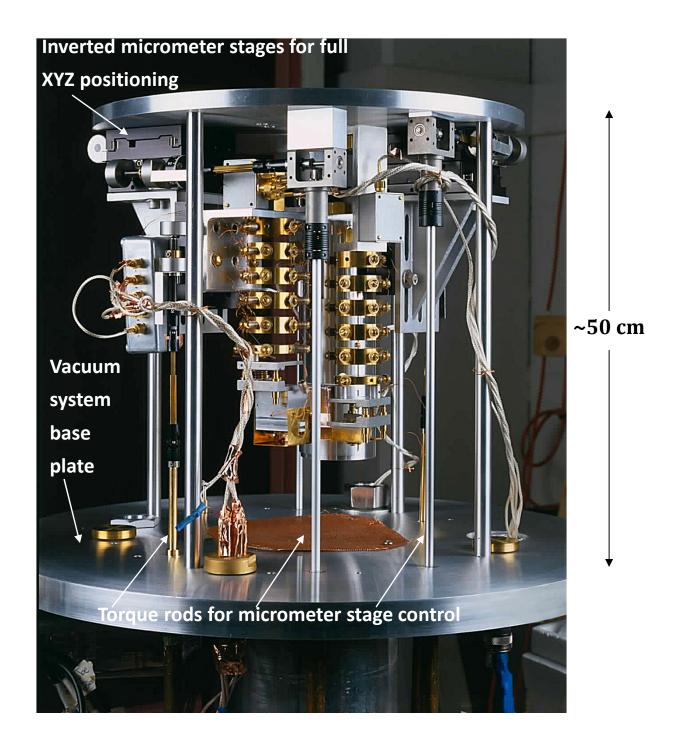
• Gravity unifies with EW force (M* ~ 1 TeV) if n = 2, $R \sim 1$ mm n = 3, $R \sim 1$ nm

Challenge: Scaling with Size of Apparatus



Background Forces: $\sim r^{-2}$ (electrostatics), $\sim r^{-4}$ (magnetic dipoles, Casimir)

Central Apparatus



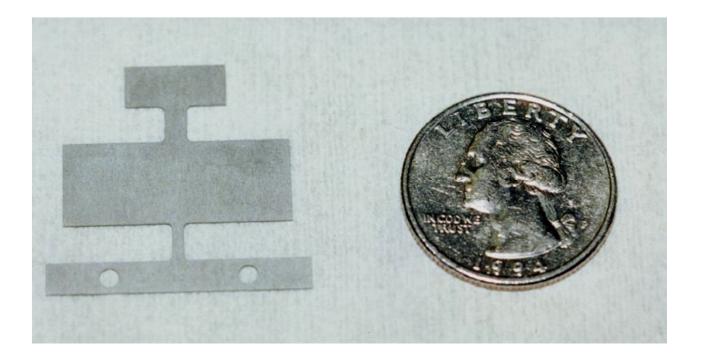
Installation at IUCEEM

Vacuum System

- Hollow riser for magnetic isolation
- LN₂ trapped diffusion pump mounts below plate
- $P \sim 10^{-7}$ torr



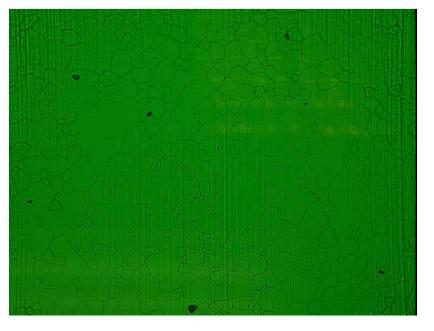
New detector prototypes have been fabricated



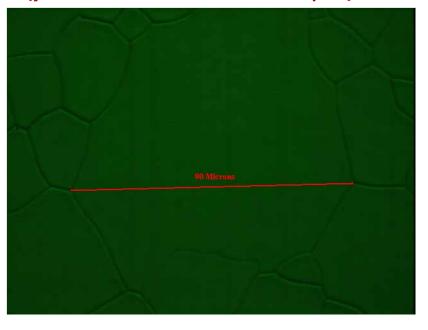
- 200 µm thick tungsten sheet (high density)
- Fabricated by wire EDM
- First generation: Annealed at 1600 K in helium atmosphere
- New oscillators: Annealed at 2700 K; expect larger crystals, higher Q

2700 K annealing leads to much larger crystals

New detector surface (200 x magnification)



1000 x showing 90 μ m crystal (previous maximum = 15 μ m)



Higher T anneals had expected material effect, but mechanical properties still under test...

New detectors and projected sensitivity

Available prototypes

Material	Q @ 300 K	Q @ 77 K	Q @ 4 K
Si	6 x 10 ³	1 x 10 ⁵	8 x 10 ⁵
W (as machined)	7 x 10 ³	1 x 10 ³	1.2 x 10 ⁴
W (1600 K anneal)*	2.5 x 10 ⁴		
W (2700 K anneal)	2.8 x 10 ⁴	1.8x 10 ⁵	1x10 ⁶ (8K)

*Used for published experiment

Data of W. Duffy (~ 3 cm diameter, 1 kHz cylindrical torsional oscillators):

J. Appl. Phys. 72 (1992) 5628

Material	Q @ 300 K	Q @ 77 K	Q@4K
W (as machined)	2 x 10 ⁴	1 x 10 ⁵	5 x 10⁵
W (2023 K anneal)	2 x 10⁵	1 x 10 ⁶	1 x 10 ⁷

 $\alpha \sim \sqrt{T/Q}$ improves by factor of 50 at 4 K

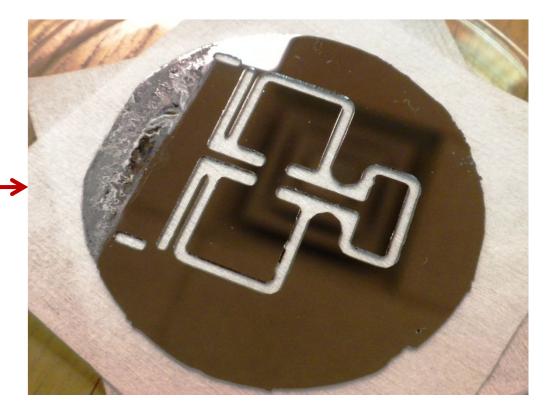
New detectors and projected sensitivity

Thinner test masses

Reduce Newtonian background

Solid, 30 µm W too flimsy

200 μm Si with 30 μm gold plate S. Jacobson, IU Chemistry

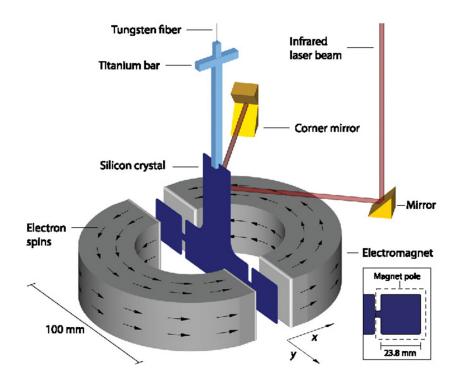


Available prototypes

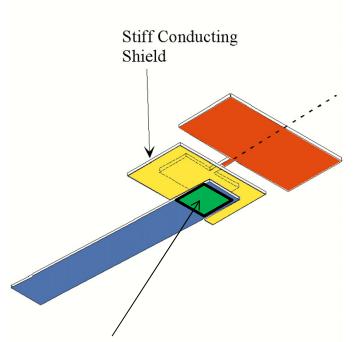
Material	Q @ 300 K	Q @ 77 K	Q@4K
Si	6 x 10 ³	1 x 10⁵	8 x 10 ⁵
W (2700 K anneal)	2.8 x 10 ⁴	1.8x 10 ⁵	1x10 ⁶ (8K)
Si (new)	1.0 x 10 ⁴	?	?

Spin – Dependent Interactions

Eot-Wash ALP torsion pendulum



S. Hoedl et al., PRL 106 (2011) 041801



Compensated test mass (Dy₆Fe₂₃)

Assume 10% of attained spin densities

- 1 mm thick
- Magnetic shield
 - μ-metal?
 - \sim 100 μm thick

Eot-Wash Torsion Pendulum Experiment D. Kapner, E. Adelberger et al., PRL 98 021101 (2007) tungsten fiber mirror for optical readout 5 cm detector mass (Mo) . source mass disks (Mo, Ta)

- 55 μ m minimum gap
- 10 μm BeCu membrane (not shown)

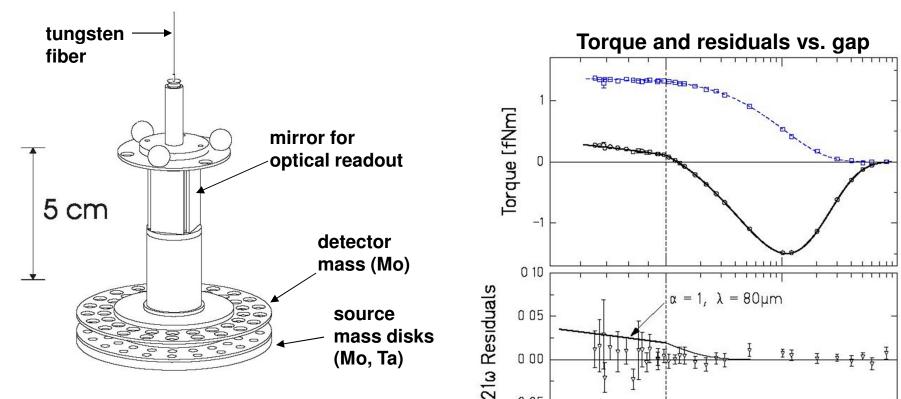
Eot-Wash Torsion Pendulum Experiment

D. Kapner, E. Adelberger et al., PRL 98 021101 (2007)

-0 05

0 05

0 07



- 55 μ m minimum gap
- 10 μm BeCu membrane (not shown)

Limits: Scenarios with $\alpha \ge 1$ excluded at 95% CL for $\lambda \ge 56 \ \mu m$

Largest extra dimension: $R < 44 \ \mu m$

ADD Model (2 equal-sized extra dimensions compactified on a torus): $R < 56 \ \mu m \Rightarrow M^* \ge 3.2 \ TeV$

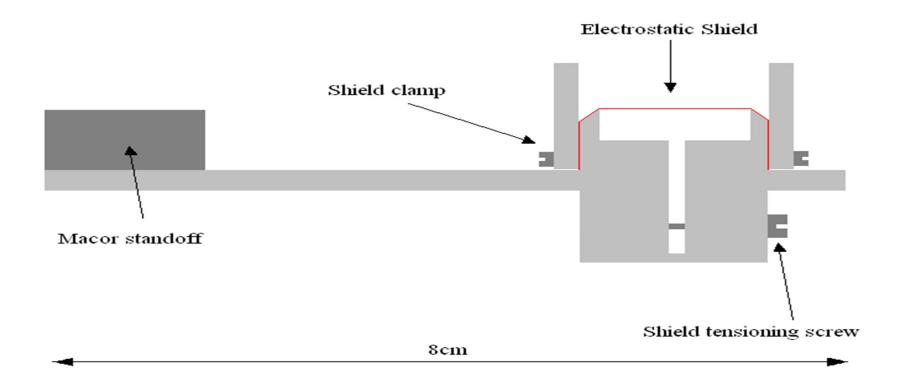
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s [mm]

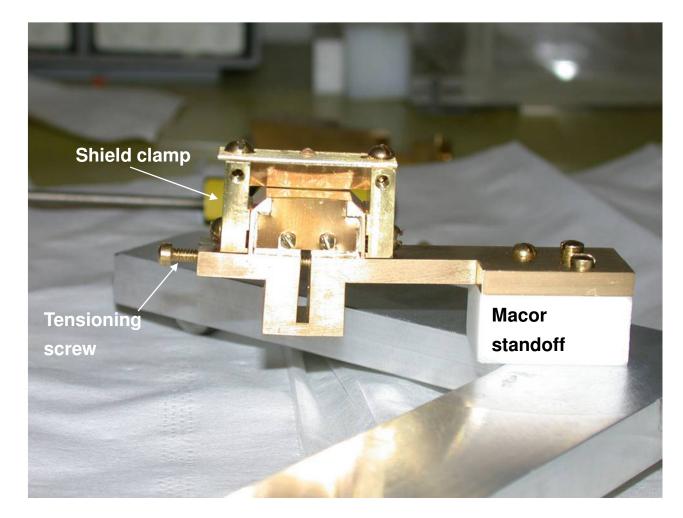
10

Stretched membrane shield is designed...

- Copper- beryllium alloy stretched over frame
- Ten microns thick
- Hourglass shape for uniform distribution of tension



Shield prototype exists and may be useable



Surface variations:

$5 \,\mu m$ peaks

0.7 μ m rms variations (should be sufficient for ~ 30 μ m experiment)

• Conducting planes surround both test masses on 5 sides (get rid of copper tape)

• 11/06: minimum gap = 48 microns

The Reality: Background forces took ~ 2 years to characterize and suppress in 1st experiment; will probably arise again at shorter ranges

Vibrations

Filter with passive isolation stacks

Check that signals are geometry independent

Residual Gas

Suppress with shield, high vacuum

Study with vacuum control

Magnetic Forces (contaminants, eddy currents)

Use non-magnetic materials

Study with applied gradients, insulating test masses

Electrostatic forces

Suppress with shield

Study with applied potentials, capacitance measurements, geometry

Systematic Errors

Parameter	Mean	Error	Units
Gravitational constant, G	6.673×10^{-11}	$1.0 imes 10^{-13}$	$\mathrm{m}^{3}\mathrm{kg}^{-1}\mathrm{s}^{-2}$
Boltzmann constant, k_B	$1.3806503 \times 10^{-23}$	2.4×10^{-29}	$J \ K^{-1}$
Detector density (tungsten), ρ_d	$1.93 imes10^4$	1.9×10^3	$\rm kg \ m^{-3}$
Source density (tungsten), ρ_s	$1.93 imes 10^4$	1.9×10^3	$\rm kg \ m^{-3}$
Thermal noise voltage, $\sqrt{ V^T ^2}$	$6.09 imes10^{-5}$	2.3×10^{-6}	V
Mechanical quality factor, Q	2.5522×10^4	29	(NA)
Resonant frequency, $\omega_0/2\pi$	1173.085	0.015	Hz
Temperature, T	305.0	0.1	Κ
Integrated rms free modeshape, $\sqrt{\int d^3 \vec{r'} \left \vec{z}^F(\vec{r'}) \right ^2}$	5.87×10^{-11}	5.9×10^{-12}	$m^{5/2}$

Parameter	Mean (m)	Error (m)
Detector length, l_d	$5.0800 imes 10^{-3}$	6.4×10^{-6}
Detector width, w_d	$1.14550 imes 10^{-2}$	6.4×10^{-6}
Detector thickness, t_d	$1.950 imes10^{-4}$	6.4×10^{-6}
Source width, w_s	$7.0000 imes 10^{-3}$	6.4×10^{-6}
Source thickness, t_s	3.048×10^{-4}	6.4×10^{-6}
Touch gap, g_{sd}	1.080×10^{-4}	6.4×10^{-6}
Source amplitude, dz_s	1.87×10^{-5}	$3.2 imes 10^{-6}$

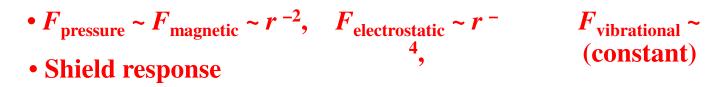
Consistency checks

Additional runs:

Larger test mass gap

Source over opposite side of detector (and shield)

Reduced overlap

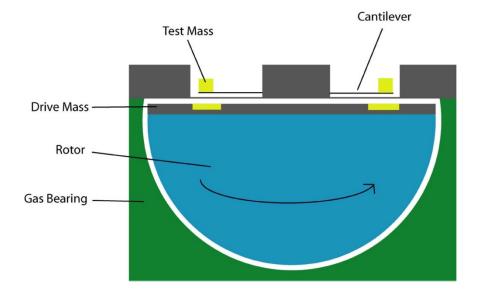


No resonant signal observed

Expected backgrounds from ambient fields: Magnetic Background = Signal with applied $B \times (B_{ambient}/B_{applied})^2 = 10^{-7} V$ ES Background = Signal with applied $V \times (V_{ambient}/V_{applied})^4 = 10^{-10} V$

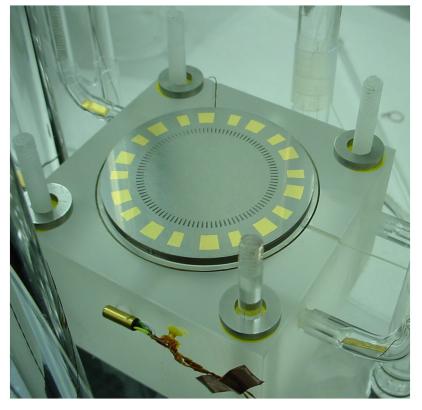
All < thermal noise $(10^{-6} V)$

Stanford Microcantilever Experiment – Generation II



- Masses modulated on spinning rotor
- Larger area drive and test masses for increased sensitivity

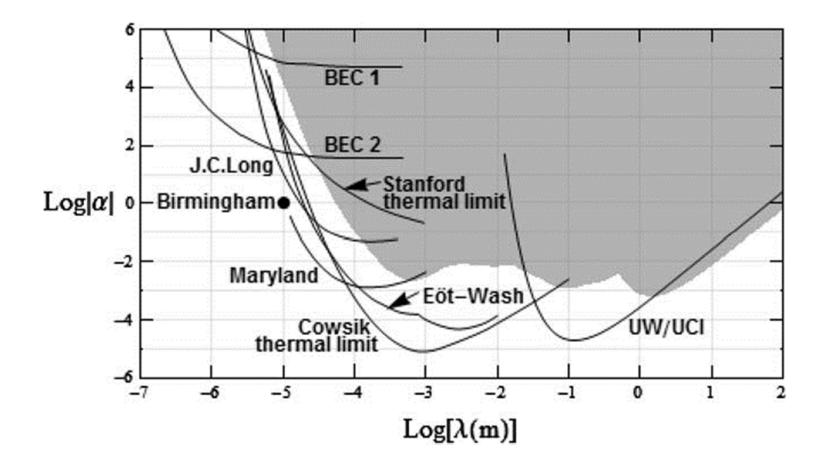
Drive mass mounted in gas bearing



figures courtesy of David M. Weld

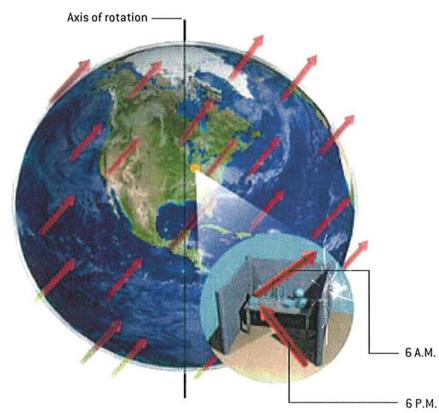
Limits and Projections – 1 μ m – 1 m

R. Newman, Space Sci. Rev. 148 (2009) 175



Search for Lorentz Violation

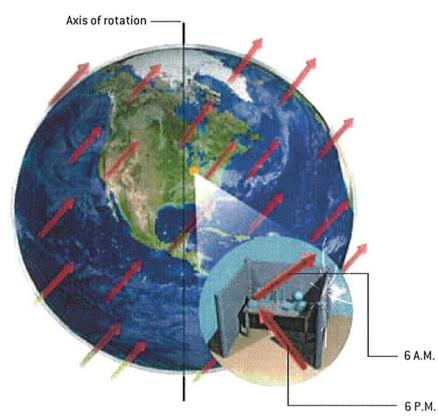
Test for sidereal variation in force signal:



Source: A. Kostelecký, Scientific American, September 2004, 93.

Search for Lorentz Violation

Test for sidereal variation in force signal:



Source: A. Kostelecký, Scientific American, September 2004, 93.

Standard Model Extension (SME)

Recently expanded to gravitational sector

V. A. Kostelecký, PRD 69 105009 (2004).

Q. G. Bailey and V. A. Kostelecký, PRD 74 045001 (2006).

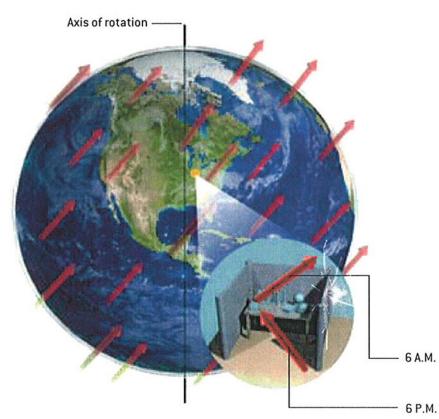
Action:

$$S = S_{GR} + S_{LV} + S_{MATTER}$$
$$S_{LV} = f(\underline{u}, s^{\mu\nu}, t^{\kappa\lambda\mu\nu})$$
20 coefficients controlling L.V.

Estimated sensitivities: $10^{-15} - 10^{-4}$

New Analysis - Search for Lorentz Violation (2002 Data)

Test for sidereal variation in force signal:



Source: A. Kostelecký, Scientific American, September 2004, 93.

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V. A. Kostelecký, PRD 69 105009 (2004).

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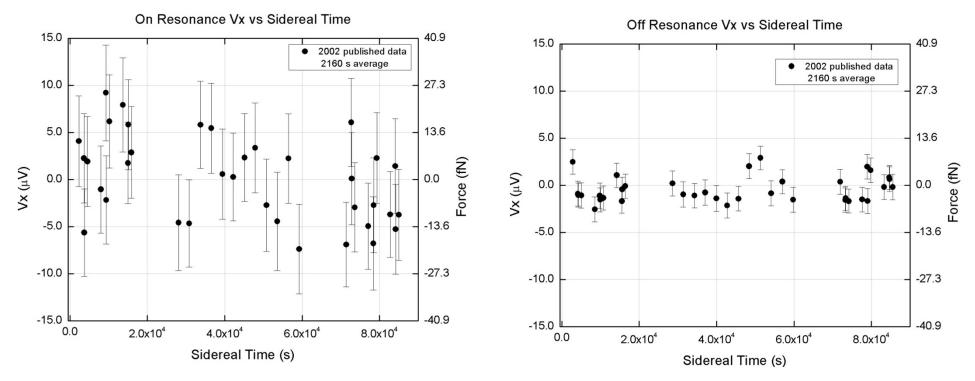
2002 Data as Function of Time

• 22 hrs of data accumulated over 5 days (August 2002)

• On-resonance (signal) data accumulated in 12 minute sets (off-resonance, diagnostic data in between)

• Plots:

Average signal over 3 consecutive sets (best for viewing time distribution) with 1σ error, vs mean time of the sets



• LV force function [1]:

]:
$$dF^{\hat{j}} = Gdm_1 dm_2 \left(-\frac{x^{\hat{j}}}{x^3} - \frac{3}{2} \frac{x^{\hat{j}}}{x^5} x^{\hat{j}} x^{\hat{k}} \bar{s}^{\hat{i}\hat{k}} + \frac{x^{\hat{k}} \bar{s}^{\hat{j}\hat{k}}}{x^3} \right)$$
$$\overline{s}^{\hat{j}\hat{k}} = \text{coefficients of Lorentz violation in the SME standard lab frame}$$
$$(x_L = \text{South}, y_L = \text{East}, z_L = \text{vertical})$$

[1] Q. G. Bailey and V. A. Kostelecký, PRD 74 045001 (2006).

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Force misaligned relative to $\vec{r} = \vec{x}_1 - \vec{x}_2$, but 1/r² behavior preserved

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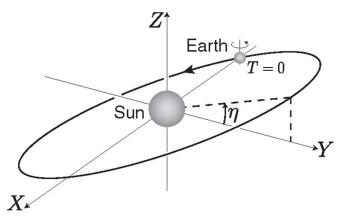
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Force misaligned relative to $\vec{r} = \vec{x}_1 - \vec{x}_2$, but 1/r² behavior preserved

• Transform to sun-centered frame [2]:



$$R = \begin{pmatrix} \cos\chi\cos\omega_{\oplus}T\,\cos\chi\sin\omega_{\oplus}T - \sin\chi\\ -\sin\omega_{\oplus}T\,\cos\omega_{\oplus}T\,& 0\\ \sin\chi\cos\omega_{\oplus}T\,\sin\chi\sin\omega_{\oplus}T\,\cos\chi \end{pmatrix}$$

 ω_{\oplus} = sidereal frequency ignore boost (η); χ = colatitude = 0.87

[1] Q. G. Bailey and V. A. Kostelecký, PRD 74 045001 (2006).
[2] V. A. Kostelecký and M. Mewes, PRD 66 056005 (2002).

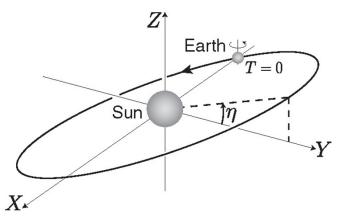
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$$F = \frac{1}{|z_{\max}|} \int_D d^3 \vec{x} \vec{z}^F(\vec{x}) \cdot dF^{\hat{j}}(\vec{x})$$

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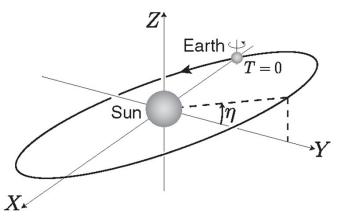
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mode shape from finite element model

[1] Q. G. Bailey and V. A. Kostelecký, PRD 74 045001 (2006).

[2] V. A. Kostelecký and M. Mewes, PRD 66 056005 (2002).

Results

D. Bennett, V. Skavysh, J. Long, Proc. 5th CPT conference

• Force:

$$\begin{split} F &= C_0 + S_\omega \sin(\omega_{\oplus} T) + C_\omega \cos(\omega_{\oplus} T) + S_{2\omega} \sin(2\omega_{\oplus} T) + C_{2\omega} \cos(2\omega_{\oplus} T) \\ C_{\omega}, S_\omega \text{ functions of detector geometry, } s^{JK} \end{split}$$

Component	Amplitude (×10 ⁻¹⁶ N)
C_0	$1.12\bar{s}^{XX} + 0.00\bar{s}^{XY} - 7.78\bar{s}^{XZ} - 3.48\bar{s}^{YY} + 0.00\bar{s}^{YZ} - 0.21\bar{s}^{ZZ}$
S_{ω}	$0.07\bar{s}^{XX} + 0.76\bar{s}^{XY} + 0.02\bar{s}^{XZ} + 0.00\bar{s}^{YY} - 0.64\bar{s}^{YZ} - 0.07\bar{s}^{ZZ}$
C_{ω}	$-0.49\bar{s}^{XX} + 0.11\bar{s}^{XY} - 0.17\bar{s}^{XZ} + 0.00\bar{s}^{YY} - 0.09\bar{s}^{YZ} + 0.49\bar{s}^{ZZ}$
$S_{2\omega}$	$0.06\bar{s}^{XX} - 0.08\bar{s}^{XY} + 0.15\bar{s}^{XZ} - 0.16\bar{s}^{YY} - 0.10\bar{s}^{YZ} - 0.09\bar{s}^{ZZ}$
$C_{2\omega}$	$0.03\bar{s}^{XX} + 0.20\bar{s}^{XY} + 0.06\bar{s}^{XZ} - 0.06\bar{s}^{YY} + 0.24\bar{s}^{YZ} + 0.04\bar{s}^{ZZ}$

• Fit:

Mean and error (2σ)	Coefficient
$(-0.04 \pm 4.90) \times 10$	\bar{s}^{XX}
$(-0.07 \pm 6.12) \times 10^{-10}$	\bar{s}^{XY}
$(-0.01 \pm 2.56) \times 10$	\bar{s}^{XZ}
$(-0.06 \pm 5.83) \times 10$	\bar{s}^{YZ}
$(0.08 \pm 6.68) \times 10^{-10}$	\overline{s}^{ZZ}

Compare: Chung, Chu, et al., PRD 80 016002: $S^{JK} < 1 \times 10^{-8}$ (atom interferometer sensitive to $\Delta g/g \sim 1 \times 10^{-9}$)